

Παράρτημα Ι. Πίνακες Χαρακτήρων των Ομάδων Σημείου

1. Οι μη περιστροφικές ομάδες σημείου C_1 , C_s και C_i

C_1	E
A	1

C_s	E	σ_h		
A'	1	1	x, y, R_z	x^2, y^2, z^2, xy
A''	1	-1	z, R_x, R_y	yz, xz

C_i	E	i		
A_g	1	1	R_x, R_y, R_z	$x^2, y^2, z^2, xy, xz, yz$
A_u	1	-1	x, y, z	

2. Οι ομάδες σημείου C_n

C_2	E	C_2		
A	1	1	z, R_z	x^2, y^2, z^2, xy
B	1	-1	x, y, R_x, R_y	yz, xz

C_3	E	C_3	C_3^2		$\epsilon = \exp(2\pi i/3)$
A	1	1	1	z, R_z	$x^2 + y^2, z^2$
E	$\begin{Bmatrix} 1 & \epsilon & \epsilon^* \\ 1 & \epsilon^* & \epsilon \end{Bmatrix}$			$(x, y); (R_x, R_y)$	$(x^2 - y^2, xy); (yz, xz)$

C_4	E	C_1	C_2	C_4^3		
A	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1		$x^2 - y^2, xy$
E	$\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$				$(x, y); (R_x, R_y)$	(yz, xz)

C_5	E	C_5	C_5^2	C_5^3	C_5^4		$\epsilon = \exp(2\pi i/5)$
A	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
E_1	$\begin{Bmatrix} 1 & \epsilon & \epsilon^2 & \epsilon^{2*} & \epsilon^* \\ 1 & \epsilon^* & \epsilon^{2*} & \epsilon^2 & \epsilon \end{Bmatrix}$					$(x, y); (R_x, R_y)$	(yz, xz)
E_2	$\begin{Bmatrix} 1 & \epsilon^2 & \epsilon^* & \epsilon & \epsilon^{2*} \\ 1 & \epsilon^{2*} & \epsilon & \epsilon^* & \epsilon^2 \end{Bmatrix}$						$(x^2 - y^2, xy)$

C_6	E	C_6	C_3	C_2	C_3^2	C_6^5		$\epsilon = \exp(2\pi i/6)$
A	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1	1	-1		
E_1	$\begin{Bmatrix} 1 & \epsilon & -\epsilon^* & -1 & -\epsilon & \epsilon^* \\ 1 & \epsilon^* & -\epsilon & -1 & -\epsilon^* & \epsilon \end{Bmatrix}$						(x, y) (R_x, R_y)	(xz, yz)
E_2	$\begin{Bmatrix} 1 & -\epsilon^* & -\epsilon & 1 & -\epsilon^* & -\epsilon \\ 1 & -\epsilon & -\epsilon^* & 1 & -\epsilon & -\epsilon^* \end{Bmatrix}$							$(x^2 - y^2, xy)$

C_7	E	C_7	C_7^2	C_7^3	C_7^4	C_7^5	C_7^6		$\epsilon = \exp(2\pi i/7)$
A	1	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
E_1	$\begin{Bmatrix} 1 & \epsilon & \epsilon^2 & \epsilon^3 & \epsilon^{3*} & \epsilon^{2*} & \epsilon^* \\ 1 & \epsilon^* & \epsilon^{2*} & \epsilon^{3*} & \epsilon^3 & \epsilon^2 & \epsilon \end{Bmatrix}$							(x, y) (R_x, R_y)	(xz, yz)
E_2	$\begin{Bmatrix} 1 & \epsilon^2 & \epsilon^{3*} & \epsilon^* & \epsilon & \epsilon^3 & \epsilon^{2*} \\ 1 & \epsilon^{2*} & \epsilon^3 & \epsilon & \epsilon^* & \epsilon^{3*} & \epsilon^2 \end{Bmatrix}$								$(x^2 - y^2, xy)$
E_3	$\begin{Bmatrix} 1 & \epsilon^3 & \epsilon^* & \epsilon^2 & \epsilon^{2*} & \epsilon & \epsilon^{3*} \\ 1 & \epsilon^{3*} & \epsilon & \epsilon^{2*} & \epsilon^2 & \epsilon^* & \epsilon^3 \end{Bmatrix}$								

C_8	E	C_8	C_4	C_2	C_4^3	C_8^3	C_8^5	C_8^7		$\epsilon = \exp(2\pi i/8)$
A	1	1	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
B	1	-1	1	1	1	-1	-1	1		
E_1	$\begin{Bmatrix} 1 & \epsilon & i & -1 & -i & -\epsilon^* & -\epsilon & \epsilon^* \\ 1 & \epsilon^* & -i & -1 & i & -\epsilon & -\epsilon^* & \epsilon \end{Bmatrix}$								$(x, y); (R_x, R_y)$	(xz, yz)
E_2	$\begin{Bmatrix} 1 & i & -1 & 1 & -1 & -i & i & -i \\ 1 & -i & -1 & 1 & -1 & i & -i & i \end{Bmatrix}$									$(x^2 - y^2, xy)$
E_3	$\begin{Bmatrix} 1 & -\epsilon & i & -1 & -i & \epsilon^* & \epsilon & -\epsilon^* \\ 1 & -\epsilon^* & -i & -1 & i & \epsilon & \epsilon^* & -\epsilon \end{Bmatrix}$									

3. Οι ομάδες σημείου D_n

D_2	E	$C_2(z)$	$C_2(y)$	$C_2(x)$		
A	1	1	1	1		x^2, y^2, z^2
B_1	1	1	-1	-1	z, R_z	xy
B_2	1	-1	1	-1	y, R_y	xz
B_3	1	-1	-1	1	x, R_x	yz

D_3	E	$2C_3$	$3C_2$		
A_1	1	1	1		$x^2 + y^2, z^2$
A_2	1	1	-1	z, R_z	
E	2	-1	0	$(x, y); (R_x, R_y)$	$(x^2 - y^2, xy); (xz, yz)$

D_4	E	$2C_4$	$C_2(=C_4^2)$	$2C_2'$	$2C_2''$		
A_1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
A_2	1	1	1	-1	-1		$x^2 - y^2$
B_1	1	-1	1	1	-1		xy
B_2	1	-1	1	-1	1		(xz, yz)
E	2	0	-2	0	0	$(x, y); (R_x, R_y)$	(xz, yz)

D_5	E	$2C_5$	$2C_5^2$	$5C_2$		
A_1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
A_2	1	1	1	-1		(xz, yz)
E_1	2	$2\cos 72^\circ$	$2\cos 144^\circ$	0	$(x, y); (R_x, R_y)$	(xz, yz)
E_2	2	$2\cos 144^\circ$	$2\cos 72^\circ$	0		$(x^2 - y^2, xy)$

D_6	E	$2C_6$	$2C_3$	C_2	$3C_2'$	$3C_2''$		
A_1	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
A_2	1	1	1	1	-1	-1		$x^2 - y^2$
B_1	1	-1	1	-1	1	-1		xy
B_2	1	-1	1	-1	-1	1		(xz, yz)
E_1	2	1	-1	-2	0	0	$(x, y); (R_x, R_y)$	(xz, yz)
E_2	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$

4. Οι ομάδες σημείου C_{nv}

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v'(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz

C_{3v}	E	$3\sigma_v$	$2C_3$		
A_1	1	1	1	z	$x^2 + y^2, z^2$
A_2	1	-1	1	R_z	
E	2	0	-1	$(x, y); (R_x, R_y)$	$(x^2 - y^2, xy); (xz, yz)$

C_{4v}	E	$2C_4$	C_2	$2\sigma_v$	$2\sigma_d$	
A_1	1	1	1	1	1	z
A_2	1	1	1	-1	-1	R_z
B_1	1	-1	1	1	-1	$x^2 - y^2$
B_2	1	-1	1	-1	1	xy
E	2	0	-2	0	0	$(x, y); (R_x, R_y)$
						(xz, yz)

C_{5v}	E	$2C_5$	$2C_5^2$	$5\sigma_v$		
A_1	1	1	1	1	z	$x^2 + y^2, z^2$
A_2	1	1	1	-1	R_z	
E_1	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	$(x, y); (R_x, R_y)$	(xz, yz)
E_2	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0		$(x^2 - y^2, xy)$

C_{6v}	E	$2C_6$	$2C_3$	C_2	$3\sigma_v$	$3\sigma_d$		
A_1	1	1	1	1	1	1	z	$x^2 + y^2, z^2$
A_2	1	1	1	1	-1	-1	R_z	
B_1	1	-1	1	-1	1	-1		
B_2	1	-1	1	-1	-1	1		
E_1	2	1	-1	-2	0	0	$(x, y); (R_x, R_y)$	(xz, yz)
E_2	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$

5. Οι ομάδες σημείου C_{nh}

C_{2h}	E	C_2	i	σ_h		
A_g	1	1	1	1	R_z	x^2, y^2, z^2, xy
B_g	1	-1	1	-1	R_x, R_y	xz, yz
A_u	1	1	-1	-1	z	
B_u	1	-1	-1	1	x, y	

C_{3h}	E	C_3	C_3^2	σ_h	S_3	S_3^5		$\epsilon = \exp(2\pi i/3)$
A'	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
E'	$\begin{Bmatrix} 1 & \epsilon & \epsilon^* \\ 1 & \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon & \epsilon^* \\ \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon^* & \epsilon \\ \epsilon & \epsilon^* \end{Bmatrix}$	1	$\begin{Bmatrix} \epsilon & \epsilon^* \\ \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon^* & \epsilon \\ \epsilon & \epsilon^* \end{Bmatrix}$	(x, y)	$(x^2 - y^2, xy)$
A''	1	1	1	-1	-1	-1	z	
E''	$\begin{Bmatrix} 1 & \epsilon & \epsilon^* \\ 1 & \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon & \epsilon^* \\ \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon^* & \epsilon \\ \epsilon & \epsilon^* \end{Bmatrix}$	-1	$\begin{Bmatrix} -\epsilon & -\epsilon^* \\ -\epsilon^* & -\epsilon \end{Bmatrix}$	$\begin{Bmatrix} -\epsilon^* & -\epsilon \\ -\epsilon & -\epsilon^* \end{Bmatrix}$	(R_x, R_y)	(xz, yz)

C_{4h}	E	C_4	C_2	C_4^3	i	S_4^3	σ_h	S_4		
A_g	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
B_g	1	-1	1	-1	1	-1	1	-1		$x^2 - y^2, xy$
E_g	$\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$	$\begin{Bmatrix} i & -i \\ -i & i \end{Bmatrix}$	$\begin{Bmatrix} -1 & 1 \\ 1 & -1 \end{Bmatrix}$	$\begin{Bmatrix} -i & i \\ i & -i \end{Bmatrix}$	1	$\begin{Bmatrix} i & -i \\ -i & i \end{Bmatrix}$	$\begin{Bmatrix} -1 & 1 \\ 1 & -1 \end{Bmatrix}$	$\begin{Bmatrix} -i & i \\ i & -i \end{Bmatrix}$	(R_x, R_y)	(xz, yz)
A_u	1	1	1	1	-1	-1	-1	-1	z	
B_u	1	-1	1	-1	-1	1	-1	1		
E_u	$\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$	$\begin{Bmatrix} i & -i \\ -i & i \end{Bmatrix}$	$\begin{Bmatrix} -1 & 1 \\ 1 & -1 \end{Bmatrix}$	$\begin{Bmatrix} -i & i \\ i & -i \end{Bmatrix}$	-1	$\begin{Bmatrix} -i & i \\ i & -i \end{Bmatrix}$	$\begin{Bmatrix} 1 & -1 \\ -1 & 1 \end{Bmatrix}$	$\begin{Bmatrix} i & -i \\ -i & i \end{Bmatrix}$	(x, y)	

C_{5h}	E	C_5	C_5^2	C_5^3	C_5^4	σ_h	S_5	S_5^7	S_5^3	S_5^9		$\epsilon = \exp(2\pi i/5)$
A'	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
E_1'	$\left\{ \begin{array}{l} 1 \ \epsilon \ \epsilon^2 \ \epsilon^{2*} \ \epsilon^* \\ 1 \ \epsilon^* \ \epsilon^{2*} \ \epsilon^2 \ \epsilon \end{array} \right\}$					1	ϵ	ϵ^2	ϵ^{2*}	ϵ^*	(x, y)	
E_2'	$\left\{ \begin{array}{l} 1 \ \epsilon^2 \ \epsilon^* \ \epsilon \ \epsilon^{2*} \\ 1 \ \epsilon^{2*} \ \epsilon \ \epsilon^* \ \epsilon^2 \end{array} \right\}$					1	ϵ^2	ϵ^*	ϵ	ϵ^{2*}		$(x^2 - y^2, xy)$
A''	1	1	1	1	1	-1	-1	-1	-1	-1	z	
E_1''	$\left\{ \begin{array}{l} 1 \ \epsilon \ \epsilon^2 \ \epsilon^{2*} \ \epsilon^* \\ 1 \ \epsilon^* \ \epsilon^{2*} \ \epsilon^2 \ \epsilon \end{array} \right\}$					-1	$-\epsilon$	$-\epsilon^2$	$-\epsilon^{2*}$	$-\epsilon^*$	(R_x, R_y)	(xz, yz)
E_2''	$\left\{ \begin{array}{l} 1 \ \epsilon^2 \ \epsilon^* \ \epsilon \ \epsilon^{2*} \\ 1 \ \epsilon^{2*} \ \epsilon \ \epsilon^* \ \epsilon^2 \end{array} \right\}$					-1	$-\epsilon^2$	$-\epsilon^*$	$-\epsilon$	$-\epsilon^{2*}$		

C_{6h}	E	C_6	C_3	C_2	C_3^2	C_6^5	i	S_3^5	S_6^5	σ_h	S_6	S_3		$\epsilon = \exp(2\pi i/6)$
A_g	1	1	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
B_g	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1		
E_{1g}	$\left\{ \begin{array}{l} 1 \ \epsilon \ -\epsilon^* \ -1 \ -\epsilon \ \epsilon^* \\ 1 \ \epsilon^* \ -\epsilon \ -1 \ -\epsilon^* \ \epsilon \end{array} \right\}$					1	ϵ	$-\epsilon^*$	-1	$-\epsilon$	ϵ^*		(R_x, R_y)	(xz, yz)
E_{2g}	$\left\{ \begin{array}{l} 1 \ -\epsilon^* \ -\epsilon \ 1 \ -\epsilon^* \ -\epsilon \\ 1 \ -\epsilon \ -\epsilon^* \ 1 \ -\epsilon \ -\epsilon^* \end{array} \right\}$					1	$-\epsilon^*$	$-\epsilon$	1	$-\epsilon^*$	$-\epsilon$			$(x^2 - y^2, xy)$
A_u	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	z	
B_u	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1		
E_{1u}	$\left\{ \begin{array}{l} 1 \ \epsilon \ -\epsilon^* \ -1 \ -\epsilon \ \epsilon^* \\ 1 \ \epsilon^* \ -\epsilon \ -1 \ -\epsilon^* \ \epsilon \end{array} \right\}$					-1	$-\epsilon$	ϵ^*	1	ϵ	$-\epsilon^*$		(x, y)	
E_{2u}	$\left\{ \begin{array}{l} 1 \ -\epsilon^* \ -\epsilon \ 1 \ -\epsilon^* \ -\epsilon \\ 1 \ -\epsilon \ -\epsilon^* \ 1 \ -\epsilon \ -\epsilon^* \end{array} \right\}$					-1	ϵ^*	ϵ	-1	ϵ^*	ϵ			

6. Οι ομάδες σημείου D_{nh}

D_{2h}	E	$C_2(z)$	$C_2(y)$	$C_2(x)$	i	$\sigma(xy)$	$\sigma(xz)$	$\sigma(yz)$		
A_g	1	1	1	1	1	1	1	1		x^2, y^2, z^2
B_{1g}	1	1	-1	-1	1	1	-1	-1	R_z	xy
B_{2g}	1	-1	1	-1	1	-1	1	-1	R_y	xz
B_{3g}	1	-1	-1	1	1	-1	-1	1	R_x	yz
A_u	1	1	1	1	-1	-1	-1	-1		
B_{1u}	1	1	-1	-1	-1	-1	1	1	z	
B_{2u}	1	-1	1	-1	-1	1	-1	1	y	
B_{3u}	1	-1	-1	1	-1	1	1	-1	x	

D_{3h}	E	$2C_3$	$3C_2$	σ_h	$2S_3$	$3\sigma_v$		
A_1'	1	1	1	1	1	1		$x^2 + y^2, z^2$
A_2'	1	1	-1	1	1	-1	R_z	
E'	2	-1	0	2	-1	0	(x, y)	$(x^2 - y^2, xy)$
A_1''	1	1	1	-1	-1	-1		
A_2''	1	1	-1	-1	-1	1	z	
E''	2	-1	0	-2	1	0	(R_x, R_y)	(xz, yz)

Θεωρία ομάδων και μοριακή συμμετρία

D_{4h}	E	$2C_4$	C_2	$2C_2'$	$2C_2''$	i	$2S_4$	σ_h	$2\sigma_v$	$2\sigma_d$		
A_{1g}	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_{2g}	1	1	1	-1	-1	1	1	1	-1	-1		$x^2 - y^2$
B_{1g}	1	-1	1	1	-1	1	-1	1	1	-1		xy
B_{2g}	1	-1	1	-1	1	1	-1	1	-1	1		(xz, yz)
E_g	2	0	-2	0	0	2	0	-2	0	0	(R_x, R_y)	(xz, yz)
A_{1u}	1	1	1	1	1	-1	-1	-1	-1	-1		z
A_{2u}	1	1	1	-1	-1	-1	-1	-1	1	1		
B_{1u}	1	-1	1	1	-1	-1	1	-1	-1	1		
B_{2u}	1	-1	1	-1	1	-1	1	-1	1	-1		
E_u	2	0	-2	0	0	-2	0	2	0	0	(x, y)	

D_{5h}	E	$2C_5$	$2C_5^2$	$5C_2$	σ_h	$2S_5$	$2S_5^3$	$5\sigma_v$			
A_1'	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$	
A_2'	1	1	1	-1	1	1	1	-1		(x, y)	
E_1'	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0		$(x^2 - y^2, xy)$	
E_2'	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0			
A_1''	1	1	1	1	-1	-1	-1	-1	z		
A_2''	1	1	1	-1	-1	-1	-1	1		(R_x, R_y)	(xz, yz)
E_1''	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	-2	$-2 \cos 72^\circ$	$-2 \cos 144^\circ$	0			
E_2''	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	-2	$-2 \cos 144^\circ$	$-2 \cos 72^\circ$	0			

D_{6h}	E	$2C_6$	$2C_3$	C_2	$3C_2'$	$3C_2''$	i	$2S_3$	$2S_6$	σ_h	$3\sigma_d$	$3\sigma_v$		
A_{1g}	1	1	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_{2g}	1	1	1	1	-1	-1	1	1	1	1	-1	-1		$x^2 - y^2$
B_{1g}	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1		xy
B_{2g}	1	-1	1	-1	-1	1	1	-1	1	-1	-1	1		(xz, yz)
E_{1g}	2	1	-1	-2	0	0	2	1	-1	-2	0	0	(R_x, R_y)	(xz, yz)
E_{2g}	2	-1	-1	2	0	0	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$
A_{1u}	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	z	
A_{2u}	1	1	1	1	-1	-1	-1	-1	-1	-1	1	1		
B_{1u}	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1		
B_{2u}	1	-1	1	-1	-1	1	-1	1	-1	1	1	-1		
E_{1u}	2	1	-1	-2	0	0	-2	-1	1	2	0	0	(x, y)	
E_{2u}	2	-1	-1	2	0	0	-2	1	1	-2	0	0		

D_{8h}	E	$2C_8$	$2C_8^3$	$2C_4$	C_2	$4C_2'$	$4C_2''$	i	$2S_8$	$2S_4$	σ_h	$4\sigma_d$	$4\sigma_v$		
A_{1g}	1	1	1	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_{2g}	1	1	1	1	-1	-1	-1	1	1	1	1	-1	-1		
B_{1g}	1	-1	-1	1	1	1	-1	1	-1	1	1	1	-1		
B_{2g}	1	-1	-1	1	1	-1	1	1	-1	1	1	-1	1	(R_x, R_y)	(xz, yz) $(x^2 - y^2, xy)$
E_{1g}	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0	2	$\sqrt{2}$	0	-2	0	0		
E_{2g}	2	0	0	-2	2	0	0	2	0	-2	2	0	0		
E_{3g}	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0	2	$-\sqrt{2}$	0	-2	0	0		
A_{1u}	1	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	z	
A_{2u}	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	1	1		
B_{1u}	1	-1	-1	1	1	1	-1	-1	1	-1	-1	-1	1		
B_{2u}	1	-1	-1	1	1	-1	1	-1	1	-1	-1	1	-1	(x, y)	
E_{1u}	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0	-2	$-\sqrt{2}$	0	2	0	0		
E_{2u}	2	0	0	-2	2	0	0	-2	0	2	-2	0	0		
E_{3u}	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0	-2	$\sqrt{2}$	0	2	0	0		

7. Οι ομάδες σημείου D_{nd}

D_{2d}	E	$2S_4$	C_2	$2C_2'$	$2\sigma_d$		
A_1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_2	1	1	1	-1	-1		
B_1	1	-1	1	1	-1		
B_2	1	-1	1	-1	1	z	xy
E	2	0	-2	0	0	$(x, y); (R_x, R_y)$	(xz, yz)

D_{3d}	E	$2C_3$	$3C_2$	i	$2S_6$	$3\sigma_d$		
A_{1g}	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_{2g}	1	1	-1	1	1	-1		
E_g	2	-1	0	2	-1	0		
A_{1u}	1	1	1	-1	-1	-1	z	
A_{2u}	1	1	-1	-1	-1	1		
E_u	2	-1	0	-2	1	0		

D_{4d}	E	$2S_8$	$2C_4$	$2S_8^3$	C_2	$4C_2'$	$4\sigma_d$		
A_1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_2	1	1	1	1	1	-1	-1		
B_1	1	-1	1	-1	1	1	-1		
B_2	1	-1	1	-1	1	-1	1	z	
E_1	2	$\sqrt{2}$	0	$-\sqrt{2}$	-2	0	0	(x, y)	
E_2	2	0	-2	0	2	0	0		$(x^2 - y^2, xy)$
E_3	2	$-\sqrt{2}$	0	$\sqrt{2}$	-2	0	0	(R_x, R_y)	(xz, yz)

Θεωρία ομάδων και μοριακή συμμετρία

D_{5d}	E	$2C_5$	$2C_5^2$	$5C_2$	i	$2S_{10}^3$	$2S_{10}$	$5\sigma_d$		
A_{1g}	1	1	1	1	1	1	1	1	R_z (R_x, R_y)	$x^2 + y^2, z^2$
A_{2g}	1	1	1	-1	1	1	1	-1		(xz, yz) $(x^2 - y^2, xy)$
E_{1g}	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0		
E_{2g}	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0		
A_{1u}	1	1	1	1	-1	-1	-1	-1	z	
A_{2u}	1	1	1	-1	-1	-1	-1	1		
E_{1u}	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	-2	$-2 \cos 72^\circ$	$-2 \cos 144^\circ$	0	(x, y)	
E_{2u}	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	-2	$-2 \cos 144^\circ$	$-2 \cos 72^\circ$	0		

D_{6d}	E	$2S_{12}$	$2C_6$	$2S_4$	$2C_3$	$2S_{12}^5$	C_2	$6C_2'$	$6\sigma_d$			
A_1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$	
A_2	1	1	1	1	1	1	1	-1	-1		z	
B_1	1	-1	1	-1	1	-1	1	1	-1			
B_2	1	-1	1	-1	1	-1	1	-1	1	(x, y)		
E_1	2	$\sqrt{3}$	1	0	-1	$-\sqrt{3}$	-2	0	0		$(x^2 - y^2, xy)$	
E_2	2	1	-1	-2	-1	1	2	0	0			
E_3	2	0	-2	0	2	0	-2	0	0			
E_4	2	-1	-1	2	-1	-1	2	0	0			
E_5	2	$-\sqrt{3}$	1	0	-1	$\sqrt{3}$	-2	0	0	(R_x, R_y)		(xz, yz)

8. Οι ομάδες σημείου S_n

S_4	E	S_4	C_2	S_4^3		
A	1	1	1	1	R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1	z	$x^2 - y^2, xy$
E	$\begin{Bmatrix} 1 & i \\ 1 & -i \end{Bmatrix}$	$\begin{Bmatrix} i & -1 \\ -i & -1 \end{Bmatrix}$	$\begin{Bmatrix} -1 & -i \\ -1 & i \end{Bmatrix}$	$\begin{Bmatrix} -i & 1 \\ i & 1 \end{Bmatrix}$	$(x, y); (R_x, R_y)$	(xz, yz)

S_6	E	C_3	C_3^2	i	S_6^5	S_6		$\epsilon = \exp(2\pi i/3)$
A_g	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
E_g	$\begin{Bmatrix} 1 & \epsilon \\ 1 & \epsilon^* \end{Bmatrix}$	$\begin{Bmatrix} \epsilon & \epsilon^* \\ \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon^* & \epsilon \\ \epsilon & \epsilon^* \end{Bmatrix}$	$\begin{Bmatrix} 1 & \epsilon \\ \epsilon^* & 1 \end{Bmatrix}$	$\begin{Bmatrix} \epsilon & \epsilon^* \\ \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon^* & \epsilon \\ \epsilon & \epsilon^* \end{Bmatrix}$	(R_x, R_y)	$(x^2 - y^2, xy); (xz, yz)$
A_u	1	1	1	-1	-1	-1	z	
E_u	$\begin{Bmatrix} 1 & \epsilon \\ 1 & \epsilon^* \end{Bmatrix}$	$\begin{Bmatrix} \epsilon & \epsilon^* \\ \epsilon^* & \epsilon \end{Bmatrix}$	$\begin{Bmatrix} \epsilon^* & \epsilon \\ \epsilon & \epsilon^* \end{Bmatrix}$	$\begin{Bmatrix} -1 & -\epsilon \\ -\epsilon^* & -1 \end{Bmatrix}$	$\begin{Bmatrix} -\epsilon & -\epsilon^* \\ -\epsilon^* & -\epsilon \end{Bmatrix}$	$\begin{Bmatrix} -\epsilon^* & -\epsilon \\ -\epsilon & -\epsilon^* \end{Bmatrix}$	(x, y)	

S_8	E	S_8	C_4	S_8^3	C_2	S_8^5	C_4^3	S_8^7		$\epsilon = \exp(2\pi i/8)$
A	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1	1	-1	1	-1	z	
E_1	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon \\ \epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} i \\ -i \end{array} \right\}$	$\left\{ \begin{array}{l} -\epsilon^* \\ -\epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right\}$	$\left\{ \begin{array}{l} -\epsilon \\ -\epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} -i \\ i \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon^* \\ \epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} (x, y); \\ (R_x, R_y) \end{array} \right\}$	
E_2	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} i \\ -i \end{array} \right\}$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right\}$	$\left\{ \begin{array}{l} -i \\ i \end{array} \right\}$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} i \\ -i \end{array} \right\}$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right\}$	$\left\{ \begin{array}{l} -i \\ i \end{array} \right\}$		$(x^2 - y^2, xy)$
E_3	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} -\epsilon^* \\ -\epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} -i \\ i \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon \\ \epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon^* \\ \epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} i \\ -i \end{array} \right\}$	$\left\{ \begin{array}{l} -\epsilon \\ -\epsilon^* \end{array} \right\}$		(xz, yz)

9. Οι κυβικές ομάδες σημείου T , T_h , T_d , O και O_h

T	E	$4C_3$	$4C_3^2$	$3C_2$		$\epsilon = \exp(2\pi i/3)$
A	1	1	1	1		$x^2 + y^2 + z^2$
E	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon \\ \epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon^* \\ \epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$		$(2z^2 - x^2 - y^2, x^2 - y^2)$
T	3	0	0	-1	$(R_x, R_y, R_z); (x, y, z)$	(xy, xz, yz)

T_h	E	$4C_3$	$4C_3^2$	$3C_2$	i	$4S_6$	$4S_6^5$	$3\sigma_h$		$\epsilon = \exp(2\pi i/3)$
A_g	1	1	1	1	1	1	1	1		$x^2 + y^2 + z^2$
A_u	1	1	1	1	-1	-1	-1	-1		
E_g	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon \\ \epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon^* \\ \epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon \\ \epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon^* \\ \epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$		$(2z^2 - x^2 - y^2, x^2 - y^2)$
E_u	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon \\ \epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} \epsilon^* \\ \epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right\}$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right\}$	$\left\{ \begin{array}{l} -\epsilon \\ -\epsilon^* \end{array} \right\}$	$\left\{ \begin{array}{l} -\epsilon^* \\ -\epsilon \end{array} \right\}$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right\}$		
T_g	3	0	0	-1	1	0	0	-1	(R_x, R_y, R_z)	(xz, yz, xy)
T_u	3	0	0	-1	-1	0	0	1	(x, y, z)	

T_d	E	$8C_3$	$3C_2$	$6S_4$	$6\sigma_d$		
A_1	1	1	1	1	1		$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1		
E	2	-1	2	0	0		$(2z^2 - x^2 - y^2, x^2 - y^2)$
T_1	3	0	-1	1	-1	(R_x, R_y, R_z)	
T_2	3	0	-1	-1	1	(x, y, z)	(xy, xz, yz)

O	E	$6C_4$	$3C_2(=C_4^2)$	$8C_3$	$6C_2$		
A_1	1	1	1	1	1		$x^2 + y^2 + z^2$
A_2	1	-1	1	1	-1		
E	2	0	2	-1	0		$(2z^2 - x^2 - y^2, x^2 - y^2)$
T_1	3	1	-1	0	-1	$(R_x, R_y, R_z); (x, y, z)$	
T_2	3	-1	-1	0	1		(xy, xz, yz)

O_h	E	$8C_3$	$6C_2$	$6C_4$	$3C_2(=C_4^2)$	i	$6S_4$	$8S_6$	$3\sigma_h$	$6\sigma_d$		
A_{1g}	1	1	1	1	1	1	1	1	1	1		$x^2 + y^2 + z^2$
A_{2g}	1	1	-1	-1	1	1	-1	1	1	-1		$(2z^2 - x^2 - y^2, x^2 - y^2)$
E_g	2	-1	0	0	2	2	0	-1	2	0		
T_{1g}	3	0	-1	1	-1	3	1	0	-1	-1	(R_x, R_y, R_z)	
T_{2g}	3	0	1	-1	-1	3	-1	0	-1	1		(xz, yz, xy)
A_{1u}	1	1	1	1	1	-1	-1	-1	-1	-1		
A_{2u}	1	1	-1	-1	1	-1	1	-1	-1	1		
E_u	2	-1	0	0	2	-2	0	1	-2	0		
T_{1u}	3	0	-1	1	-1	-3	-1	0	1	1	(x, y, z)	
T_{2u}	3	0	1	-1	-1	-3	1	0	1	-1		

10. Οι ομάδες σημείου $C_{\infty v}$ και $D_{\infty h}$ των γραμμικών μορίων

$C_{\infty v}$	E	$2C_{\infty}^{\Phi}$...	$\infty\sigma_v$		
$A_1 \equiv \Sigma^+$	1	1	...	1	z	$x^2 + y^2, z^2$
$A_2 \equiv \Sigma^-$	1	1	...	-1	R_z	
$E_1 \equiv \Pi$	2	$2 \cos \Phi$...	0	$(x, y); (R_x, R_y)$	(xz, yz)
$E_2 \equiv \Delta$	2	$2 \cos 2\Phi$...	0		$(x^2 - y^2, xy)$
$E_3 \equiv \Phi$	2	$2 \cos 3\Phi$...	0		
...		

$D_{\infty h}$	E	$2C_{\infty}^{\Phi}$...	$\infty\sigma_v$	i	$2S_{\infty}^{\Phi}$...	∞C_2		
Σ_g^+	1	1	...	1	1	1	...	1		$x^2 + y^2, z^2$
Σ_g^-	1	1	...	-1	1	1	...	-1	R_z	
Π_g	2	$2 \cos \Phi$...	0	2	$-2 \cos \Phi$...	0	(R_x, R_y)	(xz, yz)
Δ_g	2	$2 \cos 2\Phi$...	0	2	$2 \cos 2\Phi$...	0		$(x^2 - y^2, xy)$
...		
Σ_u^+	1	1	...	1	-1	-1	...	-1	z	
Σ_u^-	1	1	...	-1	-1	-1	...	1		
Π_u	2	$2 \cos \Phi$...	0	-2	$2 \cos \Phi$...	0	(x, y)	
Δ_u	2	$2 \cos 2\Phi$...	0	-2	$-2 \cos 2\Phi$...	0		
...		

11. Οι εικοσαεδρικές ομάδες σημείου I και I_h

I	E	$12C_5$	$12C_5^2$	$20C_3$	$15C_2$		
A	1	1	1	1	1		$x^2 + y^2 + z^2$
T_1	3	$\frac{1}{2}(1 + \sqrt{5})$	$\frac{1}{2}(1 - \sqrt{5})$	0	-1	$(x, y, z); (R_x, R_y, R_z)$	
T_2	3	$\frac{1}{2}(1 - \sqrt{5})$	$\frac{1}{2}(1 + \sqrt{5})$	0	-1		
G	4	-1	-1	1	0		
H	5	0	0	-1	1		$(2z^2 - x^2 - y^2, x^2 - y^2, xy, yz, zx)$

I_h	E	$12C_5$	$12C_5^2$	$20C_3$	$15C_2$	i	$12S_{10}$	$12S_{10}^3$	$20S_6$	15σ	
A_g	1	1	1	1	1	1	1	1	1	1	$x^2 + y^2 + z^2$
T_{1g}	3	$\frac{1}{2}(1 + \sqrt{5})$	$\frac{1}{2}(1 - \sqrt{5})$	0	-1	3	$\frac{1}{2}(1 - \sqrt{5})$	$\frac{1}{2}(1 + \sqrt{5})$	0	-1	(R_x, R_y, R_z)
T_{2g}	3	$\frac{1}{2}(1 - \sqrt{5})$	$\frac{1}{2}(1 + \sqrt{5})$	0	-1	3	$\frac{1}{2}(1 + \sqrt{5})$	$\frac{1}{2}(1 - \sqrt{5})$	0	-1	
G_g	4	-1	-1	1	0	4	-1	-1	1	0	$(2z^2 - x^2 - y^2,$ $x^2 - y^2,$ $xy, yz, zx)$
H_g	5	0	0	-1	1	5	0	0	-1	1	
A_u	1	1	1	1	1	-1	-1	-1	-1	-1	
T_{1u}	3	$\frac{1}{2}(1 + \sqrt{5})$	$\frac{1}{2}(1 - \sqrt{5})$	0	-1	-3	$-\frac{1}{2}(1 - \sqrt{5})$	$-\frac{1}{2}(1 + \sqrt{5})$	0	1	(x, y, z)
T_{2u}	3	$\frac{1}{2}(1 - \sqrt{5})$	$\frac{1}{2}(1 + \sqrt{5})$	0	-1	-3	$-\frac{1}{2}(1 + \sqrt{5})$	$-\frac{1}{2}(1 - \sqrt{5})$	0	1	
G_u	4	-1	-1	1	0	-4	1	1	-1	0	
H_u	5	0	0	-1	1	-5	0	0	1	-1	